

## Sheet #440. Maximizing Profit

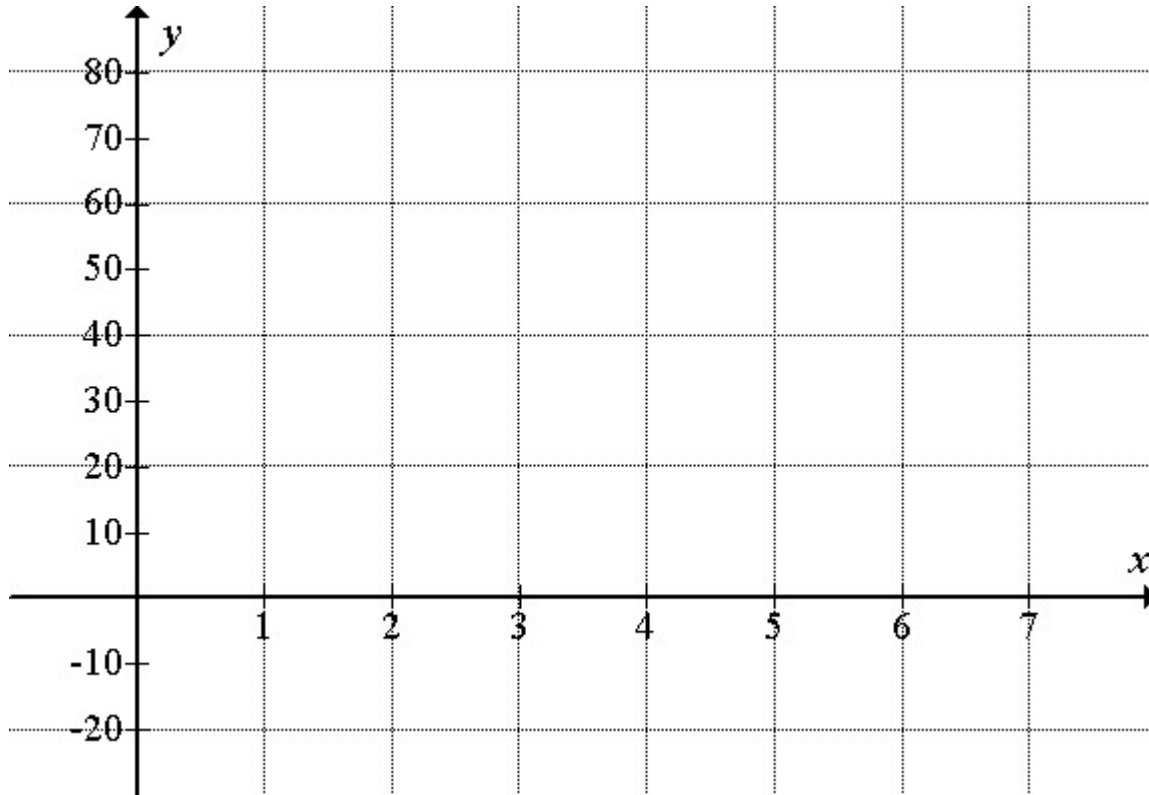
Name: \_\_\_\_\_ Period: \_\_\_\_\_

A company wants to maximize its profit. Let  $x = q$  be the number of items sold in **thousands** (same as produced).

Cost (in thousands of dollars) =  $C = x^3 - 6x^2 + 15x + 5$ .

Revenue (in thousands of dollars) =  $R = 10x$

a) Sketch the functions  $C$  and  $R$  in the window  $[0, 7]$  by  $[-20, 80]$ .



- b) What are the fixed costs?
- c) What is the price per item?
- d) For what  $x$  does the company break even?
- e) Looking at the graph you sketched, approximately for what  $x$  is the profit maximized?
- f) Use a calculator to find  $x$  at the maximum profit. What is maximum profit?
- g) Sketch the Profit =  $\Pi = R - C$  to confirm your answer.
- h) What algebraic equation do you need to solve for maximum profit? (If you run out of time, don't solve it)
- i) What is the meaning of the two solutions to the above equation?